

# **Course Description**

### MAD3107 | Discrete Structures | 3.00 credits

Topics include sets, logic, switching circuits, Boolean algebra, combinatory, probability, mathematical proofs, mathematical induction, functions, relations, and graph theory. Credit is not also given for MAD 2104. Prerequisite: MAC2312.

#### **Course Competencies:**

**Competency 1:** The student will demonstrate an understanding of set theory, logic, switching circuits, and Boolean algebra by:

- 1. Recognizing that sets, logic, and switching circuits share the properties of Boolean algebra
- 2. Performing basic operations on sets, including union, intersection, complementation, and Cartesian product
- 3. Determining the power set of a given set
- 4. Constructing truth tables of logical expressions or statements
- 5. Determining whether or not a logical statement is a tautology
- 6. Recognizing the various forms of valid arguments
- 7. Determining a logical equivalence and negating a statement involving quantifiers
- 8. Determining logical equivalences of a compound statement
- 9. Simplifying a switching circuit
- 10. Applying the properties of Boolean algebra to simplify a Boolean expression
- 11. Applying the properties of Boolean Algebra to convert a Boolean expression to conjunctive and disjunctive normal form
- 12. Proving properties of sets, logic, switching circuits, and Boolean algebra

# **Competency 2:** The student will demonstrate an understanding of combinatorics and probability by:

- 1. Counting objects in a finite set by applying sophisticated counting techniques such as the fundamental counting principle, combinations, and permutations
- 2. Counting objects in the union of finite sets using the inclusion-exclusion principle
- 3. Solving counting problems using the pigeonhole principle
- 4. Computing probabilities by counting outcomes in a sample space and in an event using combinatorics
- 5. Determining whether two or more events are mutually exclusive, independent, or dependent
- 6. Computing conditional probabilities
- 7. Computing the probability of an event within a stochastic process using a tree diagram

#### **Competency 3:** The student will demonstrate an understanding of mathematical proof by:

- 1. Writing a direct proof
- 2. Writing an indirect proof and proof by contradiction
- 3. Writing a proof by mathematical induction

# **Competency 4:** The student will demonstrate an understanding of functions and relations by:

- 1. Determining the domain, codomain, and range of a given function or relation defined between two sets
- 2. Determining whether or not a given function is an injection, surjection, or bijection
- 3. Determining the composition of two given functions
- 4. Determining the inverse of a given injection

# **Competency 5:** The student will demonstrate an understanding of graph theory by:

- 1. Identifying various types of graphs such as simple graphs, multigraphs, pseudographs, directed graphs, and directed multigraphs
- 2. Determining the number of edges and vertices of a given graph

- 3. Representing graphs by matrices
- 4. Determining whether or not two given graphs are isomorphic
- 5. Determining whether or not a given graph contains a Eulerian path and circuit
- $6.\ \$  Determining whether or not a given graph contains a Hamiltonian path and circuit

# **Learning Outcomes:**

- Use quantitative analytical skills to evaluate and process numerical data
- Solve problems using critical and creative thinking and scientific reasoning
- Use computer and emerging technologies effectively